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EXPERIMENT: The Acceleration of Gravity

The standard Physics textbook gives the value of the acceleration of gravity as $\mathbf{a} = 9.8 \text{ ms}^{-2}$

You will measure the acceleration of gravity by two completely different methods.

Method 1: You will determine **g** by measuring the period (**T**) of a simple pendulum. A simple pendulum consists of a mass at the end of a (nearly) massless string. The period **T** of such a pendulum of length **L** is given approximately by:

$$\Gamma = 2\pi \sqrt{\frac{L}{g}} \tag{1}$$



Notice that T does not depend on the mass of the pendulum. This expression for T is only accurate if the amplitude of the swing is small. For big swings, T is slightly larger than given by Eqn (1), so we will keep the amplitude to less than 5 degrees.

PROCEDURE: Measuring g with a pendulum.

The length **L** of a pendulum is the distance from the top to the CENTRE of the mass at the bottom. Adjust the length **L** of your pendulum to be close to 1.00 m and measure it as precisely as you can with a meter stick.

Set the pendulum swinging with a small amplitude, less than 5° . Measure the period **T** by using the stopwatch to measure the time for 10 complete swings and then divide by 10. Be sure to start counting from zero, not one! The *SuperMouse* software can time the swings for you.

If L = 1.000 m, you should get a value very close to 2.00 seconds for the period. A deviation of more than 0.2 seconds means that you have done something wrong. Measure T at least 4 times in order to get a good average value.

If we measure **T** as a function of **L** we can check that $T \propto \sqrt{L}$, as predicted by Eqn (1). To get rid of the square root sign we square both sides of Eqn (1):

$$T^2 = \frac{4\pi^2}{g}L$$
 (2).

This equation has the form y = m x, where $y = T^2$, $m = 4\pi^{2/3}g$, and x = L. But y = mx is the equation of a straight line with slope m that passes through the origin. So, if equation (2) is true, then a graph of T^2 vs. L should be a straight line, passing through the origin, with slope $= 4\pi^{2/3}g$.

Measure the period **T**, by timing 10 swings and dividing by 10, for at least 4 additional lengths **L** from roughly 0.2 m to 1.3 m.

Draw a graph of \mathbf{T}^2 vs. L (\mathbf{T}^2 vs. L means \mathbf{T}^2 on the y-axis, L on the x-axis.)

Measure the slope of the graph of \mathbf{T}^2 vs. **L** and compare with the predicted value of $4\pi^2/\mathbf{g}$.



Method 2: You will measure the time **t** for objects to fall a distance \mathbf{d} and determine \mathbf{g} from

$$d = \frac{1}{2}gt^2$$
(3)

PROCEDURE: Measuring g with a falling body.

When an object falls freely under the influence of gravity alone, it falls with a constant acceleration, **g**. You will measure **g** by measuring the time **t** it takes a ball to fall a measured distance **d**, starting from rest, and then compute **g** from Eqn (3):

The distance **d** that the ball falls is the distance from the bottom of the ball as it hangs to the floor. Work out a system to allow one person to release the ball while another times the fall. Otherwise the **SuperMouse** software will time the fall for you.

Record your procedure for determining **d** and its uncertainty. Record the times from several trails to get a good average value of **t** and an estimate its uncertainty. Use Eqn (3) to determine the value of **g**.

QUESTIONS:

- 1. Are the two values of g (from parts 1 and 2) consistent? What is their percent discrepancy?
- 2. In method 1 of the lab, you measure T by using a stopwatch to measure the time T for 10 complete swings, and then divide by 10. Why not measure the time for *one* complete swing?
- For method 1, list two (or more) different reasons why the value of g you obtain might not exactly yield 9.8 m/s². HINT: Discuss sources of uncertainty.

